

Test of lepton universality in rare beauty quark decays

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The Standard Model

- Mathematical model that describes all fundamental particles and their interactions
- Still open questions (DM, matter-antimatter asymmetry, ...) \Rightarrow SM is not the full picture

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Quest for New Physics

The SM is thought to be the low-energy limit of a more fundamental theory at higher energy scale with new particles and interactions.

 q g ℓ LQ

- Direct production of new particles in the collision
- Easy interpretation
- Probes masses $\lt E_{\text{collision}}$

Direct approach and Indirect approach

- New (virtual) particles induce deviations from the SM predictions
- More difficult interpretation
- Probes very-high mass scales

Rare beautiful decays

• Decays involving $b \to s(d)l^+l^-$ transitions (FCNC)

◦ forbiden at tree level in the SM

Strongly suppressed in the SM, but not necessarily beyond the SM!

P. Álvarez Cartelle (U. Cambridge) LFU in $B^+ \rightarrow K^+\ell^+\ell^-$

Flavour anomalies

In recent years, we have observed an interesting set of tensions with the SM predictions

- A) In $b \to s \ell^+ \ell^-$ transitions (FCNC)
	- $\circ~$ Branching fractions of $b\to s\mu^+\mu^-$ decays
	- \circ Angular observables in $b\to s\mu^+\mu^-$ decays
	- \circ Lepton Flavour Universality tests in μ/e ratios
- B) In $b \to c \ell \nu$ transitions (tree-level)
	- \circ Lepton Flavour Universality tests in μ/τ ratios

Theory uncertainties: Exclusive decays

Unfortunately, we do not observe the quark-transition, but the hadron decay \Rightarrow We need to compute hadronic matrix elements (form-factors and decay constants)

 $b \to s \mu \mu \implies B^+ \to K^+ \mu^+ \mu^-$, $B^0 \to K^{*0} \mu^+ \mu^-$, $B_s \to \phi \mu^+ \mu^-$...

 \rightarrow Non-pertubative QCD, i.e. these are difficult to compute.

(Lattice QCD, QCD factorisation, Light-Cone sum rules...)

 \rightarrow Certain observables will profit from cancellation of these hadronic nuisances, making them more sensitive to New Physics contributions.

Branching fraction measurements

• Branching fractions consistently below the SM prediction at low $q^2 = [m(\ell^+\ell^-)]^2$ for many $b\to s\mu\mu$ processes (2-3 $\sigma)$

Angular observables

[LHCb, PRL 125 (2020) 011802] [LHCb, arXiv:2012.13241]

- Complementary constraints on NP & orthogonal experimental systematics compared to BR's
- Give access to observables with reduced dependence on hadronic effects [JHEP 1204 (2012) 104]
- Tension with the SM at the level of $\sim 3\sigma$

New Physics or QCD?

Debate on whether we can trust the SM predictions in these observables,

• Could unaccounted for $c\bar{c}$ -loop contributions mimic a NP contribution?

Lepton flavour universality tests

- In the Standard Model, couplings of the gauge bosons to leptons are independent of lepton flavour
	- \rightarrow branching fractions of e, μ and τ differ only by phase space and helicity-suppressed contributions
- Ratios of the form:

$$
R_K = \frac{BR(B^+ \to K^+ \mu^+ \mu^-)}{BR(B^+ \to K^+ e^+ e^-)} \stackrel{\text{SM}}{\cong} 1
$$

- \rightarrow Free from QCD uncertainties that may affect other observables (hadronic effects cancel in the ratio, error is $\mathcal{O}(10^{-4})$ [JHEP 07 (2007) 040])
- → QED corrections can be $\mathcal{O}(10^{-2})$ [EPJC 76 (2016) 8,440]

Any sign of lepton flavour non-universality would be smoking gun for New Physics

LFU ratios

[\[LHCb, PRL 122 \(2019\) 191801\]](http://arxiv.org/abs/1406.6482) [\[LHCb, JHEP 08 \(2017\) 055\]](https://arxiv.org/abs/1705.05802) [\[BaBar, PRD 86 \(2012\) 032012\]](https://doi.org/10.1103/PhysRevD.86.032012) [\[Belle, PRL 103 \(2009\) 171801\]](http://arxiv.org/abs/0904.0770) [\[LHCb, JHEP 05 \(2020\) 040\]](https://arxiv.org/abs/1912.08139)

Theoretical framework - Effective theory

• Can describe these interactions in terms of an effective Hamiltonian that describes the full theory at lower energies (μ)

 $\mathcal{H}_\text{eff}\sim \sum C_i(\mu)\mathcal{O}_i(\mu)$ i

 $C_i(\mu) \to$ Wilson coefficient (perturbative, short-distance physics, sensitive to $E > \mu$)

 $\mathcal{O}_i \rightarrow$ Local operators (non-perturbative, long-distance physics, sensitive to $E < \mu$)

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 \rightarrow Contributions from New Physics will modify the measured value of the Wilson coefficients present in the SM or introduce new operators

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Global fits to $b \to s\ell^+\ell^-$ observables

Best fit prefers shifted muon vector coupling $C_9^{\mu\mu}$ (or a combination $C_9^{\mu\mu}$ and axial-vector $C^{\mu\mu}_{10}$)

- LFU observables and $B^0_s\to \mu^+\mu^-$ [theoretically clean]
- Angular observables and BR's [considerable hadronic uncertainties]

Critical to improve precision in theoretically clean observables

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[similar fits by Aebischer et al. arXiv:1903.10434, Algueró et al., arXiv:1903.09578, Kowalska et al. arXiv:1903.10932, Ciuchini et al. arXiv:2011.01212, Datta et al. arXiv:1903.10086, Arbey et al. arXiv:1904.08399]

The LHCb detector

• Forward spectrometer to study b- and c-hadron decays ($2 < \eta < 5$) © LHC

- \circ Good vertex and impact parameter resolution $(\sigma (IP) = 15 + 29/p_T) \mu m$
- Excellent momentum resolution $(\sigma(m_B) \sim 25 \text{ MeV}/c^2$ for 2-body decays)
- \circ Excellent particle ID (μ ID 97% for (π → μ) misID of 1-3%)
 \circ Versatile & efficient trigger JINST 3 (2008) S080005
- Versatile & efficient trigger

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Int. J. Mod. Phys. A 30 (2015) 1530022

New R_K measurement: LFU in $B^+ \to K^+ \ell^+ \ell^-$

$$
R_K = \frac{\int_{1.1 \text{ GeV}^2}^{6.0 \text{ GeV}^2} \frac{\mathrm{d} \mathcal{B}(B^+ \to K^+ \mu^+ \mu^-)}{\mathrm{d} q^2} \mathrm{d} q^2}{\int_{1.1 \text{ GeV}^2}^{6.0 \text{ GeV}^2} \frac{\mathrm{d} \mathcal{B}(B^+ \to K^+ e^+ e^-)}{\mathrm{d} q^2} \mathrm{d} q^2}
$$

Measurement performed on full LHCb dataset, \sim twice as many B's as previous analysis

- Previously analised Run1 and 2015 $+$ 2016 data (5 fb $^{-1})$
- Added 2017 and 2018 datasets (4 fb^{-1})

Similar strategy to previous measurement [LHCb, PRL 122 (2019) 191801]

 $\bullet\,$ Same q^2 region: $\,$ [1.1, 6.0] ${\rm GeV^2\!/c^4}$

Electron Bremsstrahlung

Electrons lose a large fraction of their energy through Bremsstrahlung radiation

Bremsstrahlung recovery procedure to improve momentum measurement for electrons

 \rightarrow Add photon clusters in the calorimeter $(E_T > 75 \text{ MeV})$ compatible with electron direction before magnet

[\[LHCb, PRL 122 \(2019\) 191801\]](https://cds.cern.ch/record/2668514?)

1. Even after Bremsstrahlung recovery, electrons still have degraded momentum, and mass/ q^2 resolution

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- 2. Very different trigger signatures: Lower trigger efficiency for electrons
	- Muons identified by Muon stations
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 \rightarrow Critical aspect of the analysis: Get the differences between electron and muon efficiencies fully under control

Analysis strategy

$$
R_K = \frac{\mathcal{B}(B^+ \to K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \to K^+ J/\psi(\mu^+ \mu^-))} / \frac{\mathcal{B}(B^+ \to K^+ e^+ e^-)}{\mathcal{B}(B^+ \to K^+ J/\psi(e^+ e^-))}
$$

$$
= \frac{N(B^+ \to K^+\mu^+\mu^-)}{N(B^+ \to K^+J/\psi(\mu^+\mu^-))} \times \frac{\varepsilon_{B^+ \to K^+J/\psi(\mu^+\mu^-)}}{\varepsilon_{B^+ \to K^+\mu^+\mu^-}}
$$

$$
\times \frac{N(B^+ \to K^+ J/\psi(e^+e^-))}{N(B^+ \to K^+e^+e^-)} \times \frac{\varepsilon_{B^+ \to K^+e^+e^-}}{\varepsilon_{B^+ \to K^+ J/\psi(e^+e^-)}}
$$

- R_K is measured as a **double ratio** to cancel out most systematics $\rightarrow B^+ \rightarrow K^+ J/\psi (\ell^+ \ell^-)$ measured to be LF-universal within 0.4%
- Yields determined from a fit to the invariant mass of the final state particles
- Efficiencies computed using simulation that is calibrated with control channels in data

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Resonant and nonresonant are separated in q^2

 \rightarrow However, good overlap between $B^+ \rightarrow K^+ \ell^+ \ell^-$ and $B^+ \to K^+ J/\psi (\ell^+ \ell^-)$ in the variables relevant to the detector response

Analysis strategy

[\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

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Selection & backgrounds

[\[LHCb, PRL 122 \(2019\) 191801\]](https://cds.cern.ch/record/2668514?)

Identical selection between resonant and rare modes (except q^2 and $m(K\ell\ell))$

- \bullet Use particle ID requirements and mass vetoes to suppress exclusive B -decays to negligible levels
	- $\circ~$ Backgrounds from e.g. $B\to \bar{D}^0(K\ell\nu)\ell\nu$, with $m(K\ell)>m_{D^0}$
	- \circ Mis-ID backgrounds, e.g. $B\to K\pi_{(\to e^+)}^+\pi_{(\to e^-)}^-$, with electron ID
- Multivariate selection to reduce combinatorial background (BDT)

Remaining backgrounds suppressed by choice of $m(K\ell\ell)$ window

- $B^+ \rightarrow K^+ J/\psi (e^+ e^-)$
- Partially reconstructed $B \to K X \ell \ell$ decays
- Modelled in fit by constraining their fractions between trigger categories and calibrating simulated templates from data.
- Cross-check our estimates using control regions in data and changing $m(K\ell\ell)$ window in fit

Efficiency calibration

Ratio of efficiencies determined with simulation carefully calibrated using control channels selected from data:

- Particle ID calibration
	- Tune particle ID variables for diff. particle species using kinematically selected calibration samples $(D^{*+} \rightarrow D^0(K^-\pi^+)\pi^+...)$ [EPJ T&I(2019)6:1]
- Calibration of q^2 and $m(K^+e^+e^-)$ resolutions

 $\circ~$ Use fit to $m(J/\psi)$ to smear q^2 in simulation to match that in data

- Calibration of B^+ kinematics
- Trigger efficiency calibration

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Calibration of B^+ kinematics

- Calibrate the simulation so that it describes correctly the kinematics of the B^{+} 's produced at LHCb.
- Compare distributions in data and simulation using $B^+ \to K^+ J/\psi (\ell^+ \ell^-)$ candidates.
- Iterative reweighing of $p_T(B^+) \times \eta(B^+)$, but also the vertex quality and the significance of the B^+ displacement.

 \rightarrow Systematic uncertainty from RMS between all these weights

Cross-check: Measurement of $r_{J/\psi}$ [\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

• To ensure that the efficiencies are under control, check

$$
r_{J/\psi} = \frac{\mathcal{B}(B^+ \to K^+ J/\psi(\mu^+ \mu^-))}{\mathcal{B}(B^+ \to K^+ J/\psi(e^+ e^-))} = 1,
$$

known to be true within 0.4%.

- Very stringent check, as it requires direct control of muons vs electrons.
- Result:

$$
r_{J/\psi} = 0.981 \pm 0.020 \text{ (stat + syst)}
$$

• Checked that the value of $r_{J/\psi}$ is compatible with unity for all periods and in all trigger samples.

Cross-check: $r_{J/\psi}$ as a function of kinematics

Check that efficiencies are understood in all kinematic regions $\rightarrow r_{J/\psi}$ is flat for all variables examined

 \rightarrow e.g. given expected $\min(p_T(\ell^+), p_T(\ell^-))$ spectra, bias expected on R_K if deviations are genuine rather than fluctuations is 0.1% [\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

Cross-check: Measurement of $R_{\psi(2S)}$ [\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

• Measurement of the double ratio

$$
R_{\psi(2S)} = \frac{\mathcal{B}(B^+ \to K^+ \psi(2S)(\mu^+ \mu^-))}{\mathcal{B}(B^+ \to K^+ J/\psi(\mu^+ \mu^-))} / \frac{\mathcal{B}(B^+ \to K^+ \psi(2S)(e^+ e^-))}{\mathcal{B}(B^+ \to K^+ J/\psi(e^+ e^-))},
$$

Result well compatible with unity:

$$
R_{\psi(2S)} = 0.997 \pm 0.011 \text{ (stat + syst)}
$$

Systematics uncertainties

Dominant sources (~ 1%)

- Choice of fit model
	- Associated signal and partially reconstructed background shape
- Statistics of simulation and calibration samples
	- Bootstrapping method that takes into account correlations between calibration samples and final measurement

Sub-dominant sources $({\sim 10'_{\text{oo}}})$

- Efficiency calibration
	- Dependence with tag, in tag-and-probe determinations;
	- Parameterisation bias (e.g. factorisation of PID efficiencies for kaons and electrons) tag and trigger bias;
	- $\circ~$ Dependence of q^2 and $m(K^+e^+e^-)$ resolution with q^2
	- Inaccuracies in material description in simulation (tracking efficiency) $^{\circ}$...

 \rightarrow Total relative systematic of 1.5% in the final R_K measurement \Rightarrow Expected to be statistically dominated

Fit to the resonant modes

Yields for $B^+ \to K^+ J/\psi(\ell^+\ell^-)$, used as input for cross-checks and final determination of R_K , obtained from a fit to the J/ψ -constrained B mass

- Signal and background shapes determined from calibrated simulation
- Allow for a shift in the position in the signal peak and a scale factor to the resolution to float in the fit
- Results cross-checked with a fit to the unconstrained $m(K\ell\ell)$

Simultaneous fit to extract R_K

- Get R_K directly as a parameter of the fit
- $\bullet\,$ Perform simultaneous fit to $m(K^+e^+e^-)$ and $m(K^+\mu^+\mu^-)$ distributions

$$
R_K = \frac{N_{K\mu\mu}^r}{N_{Kee}^{rt}} \cdot \frac{N_{J/\psi ee}^{rt}}{N_{J/\psi\mu\mu}^r} \cdot \frac{\varepsilon_{Kee}^{rt}}{\varepsilon_{K\mu\mu}^r} \cdot \frac{\varepsilon_{J/\psi\mu\mu}^r}{\varepsilon_{J/\psi ee}^{rt}}
$$

$$
=\frac{N_{K\mu\mu}^{r}}{N_{Kee}^{rt}}\cdot c_{K}^{rt},
$$

for $r =$ Run 1, Run 2 and $t =$ L0Electron, L0Hadron, L0TIS.

- $\bullet \ \ c_K^{rt}$ are included as a multidimensional Gaussian constraint, with uncertainties and correlations according to the 6×6 covariance matrix σ
- Partially reconstructed background comes essentially from $B\to K\pi e^+e^-$ and so it can be constrained using

$$
\frac{N_{prc}^{r,t}}{N_{prc}^{r, e\mathrm{TOS}}} = \frac{\varepsilon_{trig,mass}^{r,t}(K\pi ee)}{\varepsilon_{trig,mass}^{r, e\mathrm{TOS}}(K\pi ee)} = r_{prc}^{rt}
$$

Fit to $B^+ \to K^+ \ell^+ \ell^-$ candidates

[\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

- Signal and background shapes determined from calibrated simulation.
- Mass shift and resolution scale fixed to that observed in the fit to the resonant mode.
- Leakage from $B^+ \to J/\psi (ee) K^+$ in the $B^+ \to K^+ e^+ e^-$ signal region $(1.1 < q^2 < 6.0 \,\text{GeV}^2/c^4)$, constrained from the fit to the resonant mode.

R_K with full Run1 and Run2 dataset

[\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

[\[Belle, JHEP 03 \(2021\) 105\]](http://arxiv.org/abs/1908.01848)

[\[BaBar, PRD 86 \(2012\) 032012\]](https://doi.org/10.1103/PhysRevD.86.032012)

 $R_K = 0.846_{-0.039}^{+0.042} \text{ (stat)}_{-0.012}^{+0.013} \text{ (syst)}$

Compatibility with the Standard Model

- Compatibility with the SM obtained by integrating the profiled likelihood as a function of R_K above 1
	- \circ Taking into account the 1% theory uncertainth on R_K [EPJC76(2016)8,440]
	- p-value is converted into significance using the inverse Gaussian c.d.f. for a one-sided conversion

- p-value under the SM hypothesis: 0.0010
- \rightarrow Evidence of LFU violation at 3.1 standard deviations

Measurement of $\mathcal{B}(B^+ \to K^+e^+e^-)$ [\[LHCb-PAPER-2021-004\]](https://arxiv.org/abs/2103.11769)

In the range $q^2 \in [1.1, 6]$ ${\rm GeV^2/}c^4$

 $d\mathcal{B}(B^+\rightarrow K^+e^+e^-)$ $\frac{d^2A^2 + R^2 e^-}{dq^2} = (28.6 \frac{11.5}{-1.4} \text{(stat)} \pm 1.4 \text{(syst)}) \times 10^{-9} \frac{c^4}{\text{GeV}^2}$

- Dominant systematic comes from the $\mathcal{B}(B^+ \to K^+J/\psi)$
- This is the most precise determination of this branching fraction to date

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New measurement of $\mathcal{B}(B_{(s)}^{0} \to \mu^+ \mu^-)$ [LHCb-PAPER-2021-007]

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Impact on Global Fits

- Best fit point still in tension with the SM
- \rightarrow Scenario with $C_9 = -C_{10}$ still good
- Tension between $R_K^{(*)}$ & $b\to s\mu^+\mu^-$ observables
- \rightarrow could be reduced by LFU contribution to C_9

[Similar fits by M. Algueró et al., Moriond QCD 2021,

C. Cornella et al., arXiv:2103.16558, L-G. Geng et al., arXiv:2103.12738]

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Connection with charged currents?

- C_9^{univ} can arise from corrections involving τ -loops
- Need to consider SMEFT (higher scale)
- Consider operators that can explain also anomalies in $b \rightarrow c \ell \nu$
	- $\rightarrow \quad R(D^{(*)})=\mathcal{B}(B\to D^{(*)}\tau\nu)/\mathcal{B}(B\to D^{(*)}\mu\nu)$
- \rightarrow Oversimplified scenario (need to consider real models)

Bobeth, Haisch, arXiv:1109.1826 Crivellin, Greub, Müller, Saturnino, arXiv:1807.02068

[\[J. Kriewald et al., arXiv:2104.00015\]](https://arxiv.org/abs/2103.13370)

What next?

LHCb Integrated Recorded Luminosity in pp. 2010-2018

- With the LHCb dataset in hand, many interesting results still to come
	- Update of R_{K*0} with full Run 2 dataset
	- \circ LFU test in different channels: $R_\phi, \, R_{K_S}, \, R_{K^{\ast +}}, \, R_{K\pi\pi} ...$
	- $\circ~$ Update of angular observables of $b\to s\mu^+\mu^-$ decays
	- \circ Measurements of $b \rightarrow s\tau\tau$ processes and LFV involving τ 's
- For a definite answer on LFU we will need Run 3, as well as input from other LHC experiments and Belle II

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Conclusions

- Performed measurement of the LFU ratio R_K using the full Run 1 and Run 2 LHCb dataset
	- **Compatibility with the SM at** $3.1\sigma \Rightarrow$ Evidence for LFU breaking
- Many more results on rare $b \rightarrow s\ell\ell$ decays on the pipeline
- Run 3 definitely needed to understand the full picture, as well as measurements from ATLAS, CMS and Belle II

