SANDA Project Subtask 5.2.1: correlations in integral experiments

V. Bécares (CIEMAT), N. García-Herranz (UPM), O. Cabellos (UPM), I. Kodeli (UKAEA), G. Zerovnik (JSI), D. Bernard (CEA)



SANDA pending deliverables meeting

Subtask 5.2.1: correlations in integral experiments

• SANDA subtask 5.2.1: Assessing correlations in integral experiments

Subtask 5.2.1: Assessing correlations in integral experiments

While a considerable effort has been given to nuclear data covariances in recent years, much less attention has been paid to correlations in integral experiments used in validation, adjustment, and assimilation studies. In point of fact, correlation coefficient data for criticality cases are available for only 93 integral experiments of the DICE database associated with the ICSBEP Handbook.

Although this project will not attempt to produce adjusted nuclear data libraries nor to assimilate validation information, CIEMAT, JSI, CEA/DEN, and UPM will share their best experts' opinions on the "missing correlations in integral experiments" problem, with the goal of assessing its impact on nuclear data validation studies. Simulations will be made to estimate the correlations between the experimental uncertainties of integral experiments and quantify their impact on some reactor concept.

• Work already performed:

- CIEMAT&UPM: literature review (next slides)
- UKAEA & JSI: correlations in shielding benchmarks (ASPIS-Fe88, PCA-REPLICA) SANDA GM
- CEA: correlations in configurations of the EOLE reactor (CAMELEON program) | March 2022
- Simulations?

• **D5.6** *Report on correlations between integral experiments* (<u>CIEMAT</u>, JSI, CEA, UPM).

Proposed structure for D5.6

- Introduction 1
- Origin of experimental correlations 2.
- 3. Impact of experimental correlations
 - 2.1. Criticality safety
 - 2.2. Reactor physics
 - 2.3. Radiation shielding
 - 2.4. Nuclear data
- Status of existing correlations 4.
- 5. Methodologies to produce correlations
 - 4.1 Expert judgement/ deterministic
 - 4.2 Monte Carlo
- 6. Applications

Status of existing correlations (I)

• Cuantitavive correlations in DICE for 93 cases (out of 5121 cases in ICSBEP)

-55 cases correspond to four sets of HEU-SOL-THERM benchmarks.

HST HST



IPPE: 21 (HST019/025/027/028/029/030/035)

T. Ivanova et al., Influence of the Correlations of Experimental Uncertainties on Criticality Prediction. NSE 145 (2003) 97–104



ORNL: 14 (HST009/ /010/011/012/043) + 10 (HST013/032/042)



006

001 001 001 001 001 001 001

001 001

CIEMAT

HST HST HST

003 004 005

001

001 002

Status of existing correlations (II)

ZPR & ZPPR @ ANL (33 cases)



G. Palmiotti *et al., Combined Use of Integral Experiments and Covariance Data*. NDS 118 (2014) 596-636.

VNIIEF (3 cases)

HMF	HMF	HMF	ICSBEP no.	Facility/core						
018 001	020 001	031 001	HMF018	CTF, bare U235 (90%) sphere						
1000	460	320		CTF. U235 (90%) sphere, PE						
460	1000	460	HMF020	reflector						
320	460	1000								
			HMF031	CTF, U235 (90%) sphere, PE central area and reflector						

VNIITF (2 cases)

	HMF	HMF
	008	011
	001	001
HMF008-001	1000	210
HMF011-001	210	1000

ICSBEP no.	Facility/core
HMF008	FKBN, HEU sphere
HMF011	FKBN, HEU sphere and PE reflector

ICSBEP no.	Facility/core	No. Cases
HMF055	ZPR-3/23	1
HMF060	ZPR-9/4	1
HMF061	ZPR-21F	1
HMF067	ZPR-9/5 & 6	2
HMF070	ZPR-9/7, 8 & 9	3
HMF075	ZPPR-20/C	1
HMI001	ZPR-9/34	1
HMM012	ZPPR-20/D	1
ICF004	ZPR-3/12	1
ICI005	ZPR-6/6A	1
IMF010	ZPR-6/9	1
IMF012	ZPR-3/41	1
IMF013	ZPR-9/1	1
IMF014	ZPR-9/2&3	2
IMF015	ZPR-3/6F	1
IMF016	ZPR-3/11	1
MCF001	ZPR-6/7	1
MCF002	ZPR-6/7 (Pu-240)	1
MCF003	ZPR-3/48	2
MCF004	ZPR-3/56	1
MMF011	ZPPR-21	4
PMF033	ZPPR-21A	1
PMI002	ZPR-6/10	1
SHMF001	ZPPR-20/E	2

HMF018-001

HMF020-001

HMF031-001

• Expert judgement / deterministic methodologies

Ivanova <i>et al.</i> (2003) Intl. Conf. Nuc. Crit. Ivanova <i>et al.</i> (2003) NSE 145 97–104	Methodology described. Correlations in k_{eff} unc. for 77 HEU-SOL-THERM cases: 34 from IPPE, 10 from Rocky Flats, 29 from ORNL and 4 from LANL. No numerical information.
Ivanova <i>et al.</i> (2009) ANE 36 305–309	Correlations in k_{eff} unc. for 10 cases from IPPE's BFS-99, 99 and 101 (MMCF003/004, MMCM001)
Dos Santos (2013) PhD Thesis Dos Santos <i>et al.</i> (2013) ANNIMA2013	Methodology described. Correlations in k_{eff} unc. for 6 systems, including 3 cases from ICSBEP (ZPR-10A(?) and MCT001).
Ivanova <i>et al.</i> (2014) NSE 178 1-15	Correlations in k_{eff} unc. for some fast benchmarks from IRPhE (ZEBRA, ZPR, SNEAK, NEA-NSC-WPEC-SG33) and thermal benchmarks for ICSBEP (LCT007-039, UACSA Benchmark Phase IV)
NEA/NSC/WPEC/DOC(2013)445 Salvatores <i>et al.</i> (2014) NDS 118 38-71	Correlations in k_{eff} unc. for ZPR-6/7 and ZPPR-9, correlations in spectral indexes in some other systems.
Palmiotti <i>et al.</i> (2014) NDS 118 596-636	Correlations in k_{eff} unc. for 33 ZPR benchmark experiments. Results of US DOE Nuclear Data Adjustment Project.
Jeong <i>et al.</i> (2017) M&C2017	Correlation matrices for some LEU-COMP-THERM and HEU-COMP-FAST cases. No numerical information.

• Monte Carlo methodologies

Buss <i>et al.</i> (2010) PHYSOR2010	Correlations in k_{eff} unc. for 97 LEU-COMP-THERM and MIX-COMP-THERM cases. MC code used: SCALE 6. No numerical information.
Stuke <i>et al.</i> (2016) GRS-440 Kilger <i>et al.</i> (2016) ANE 96 354-362	Correlations in k_{eff} unc. for 9 LCT cases (LCT006 and LCT035/062, JAEA's TCA) and 43 PST cases (PST003/006/020/21) (no numerical information). MC code used: KENO.
Marshall (2017) PhD. Thesis	Correlations in k_{eff} unc. for a series of cases of LCT007/039 (CEA Valduc), LCT042 (PNL) and HST001 (Rocky Flats) benchmarks. MC code used: KENO
Sommer & Stuke (2021) ANE 157 108209	S2Cor methodology for efficient MC sampling to calculate correlatons. Applied to some LCT007 (CEA Valduc) cases. MC code used: KENO

Comprehensive documents

Stuke [Ed.] (2016) GRS-414	Results of EG UACSA Benchmark Phase IV. Intercomparison of
Stuke <i>et al.</i> (2019) ICNC 2019	methodologies for generating correlation matrices in LCT-007 (4 cases)
NEA/NSC/R(2021)1	and LCT-039 (17 cases) (Apparatus-B @ CEA Valduc)

Missing correlations (I)

IPPE: 30 additional benchmarks in three facilities with correlated uncertainties

- BRR-1-1: 4 (PMF012 & rel.)
- KBR & BFS: 26 (experimental correlations?)

	PMM	HMF	HMI	HMI	HMT	HMM	HCI	IMF	ICF	ICI	ICI	ICT	MMF	MMF	MMCF	MMCF	MMCF	MMCF	MMCM	PMI	PMT	
	001	068	005	008	005	005	005	017	002	001	002	005	006	015	001	002	003	004	001	001	001	1
																						-
PMM001	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	(+)	
HMF068	+	(+)	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
HMI005	+	+	(+)	+	(+)	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
HMI008	+	(+)	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
HMT005	+	+	(+)	+	(+)	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
HMM005	+	+	(+)	+	(+)	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
HCI005	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	
IMF017	+	+	+	+	+	+	+	(+)	+	+	(+)	+	+	(+)	(+)	+	+	+	+	+	+	
ICF002	+	+	+	+	+	+	+	+	(+)	(+)	+	(+)	+	+	+	+	+	+	+	+	+	
ICI001	+	+	+	+	+	+	+	+	(+)	(+)	+	(+)	+	+	+	+	+	+	+	+	+	
ICI002	+	+	+	+	+	+	+	(+)	+	+	(+)	+	+	(+)	(+)	+	+	+	+	+	+	
ICT005	+	+	+	+	+	+	+	+	(+)	(+)	+	(+)	+	+	+	+	+	+	+	+	+	
MMF006	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	
MMF015	+	+	+	+	+	+	+	(+)	+	+	(+)	+	+	(+)	(+)	+	+	+	+	+	+	
MMCF001	+	+	+	+	+	+	+	(+)	+	+	(+)	+	+	(+)	(+)	+	+	+	+	+	+	
MMCF002	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	
MMCF003	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	(+)	+	+	
MMCF004	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	
MMCM001	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	(+)	+	+	
PMI001	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	(+)	
PMT001	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	(+)	
																						-

T. Ivanova <i>et al., Towards validation of criticality calculations</i>
for systems with MOX powders. ANE 36 (2009) 305-309

	Facility/core	Year			
HCI005	KBR-7/9/10/15/16	1970-90			
ICF002	KBR-18				
ICI001	KBR-19/20				
ICT005	KBR-21	1990-94			
HMF068	KBR-22				
HMI008	KBR-23				
MMCF001	BFS-31/42				
ICI002	BFS-33	4077 70			
IMF017	BFS-35	1977-79			
MMF015	BFS-38				
MMCF002	BFS-49	1985			
MMF006	BFS-61				
НММ005	BFS-79-1/2				
НМТ005	BFS-79-3	1000			
HMI005	BFS-79-4/5	1999			
PMI001	BFS-81-1/2				
PMM001	BFS-81-3				
PMT001	BFS-81-4/5	1999-2000			
MMCF003	BFS-97-1/2, BFS-101-1				
MMCF004	BFS-97-3/4, BFS-99- 1/2, BFS-101-2/3	2004-05			
MMCM001	BFS-97-5/6/7	2008-09			



Missing correlations (II)

CTF @ VNIIEF (34 bench. in 6 groups)

- 1. Pu(98%)/U(90%): 2 (MMF009-010)
- 2. U(90%): 10 (HMF018 & rel.)
- 3. Pu(89%): 5 (PMF029 & rel.)
- 4. U(36%): 6 (IMF003 & rel.)
- 5. Pu(98%): 9 (PMF022 & rel.)
- 6. Pu(88%): 2 (PMF027-028)

FKBN @ VNIITF (54 bench. in 4 groups)

- 1. U/Pu, cyl. conf.: 40 (HMF015 & rel.)
- 2. HEU, sph. conf.: 8 (HMF008 & rel.)
- 3. Pu, cyl. & sph. confs.: 3 (PMF019-021)
- 4. Pu/HEU, sph. conf.: 3 (MMF003-005)

Correlations for a few cases included in DICE.

Missing correlations (III)



Kurchatkov inst. (30 bench. in 6 groups)

- 1. SF-9: 8 (LCT053 & rel.)
- 2. Tank facility: 5 (LCT022-025, LCT032)
- 3. Tank facility: 4 (HCT011-014)

- 4. Narciss-M: 3 (HCM003-004, HCT009)
- 5. Tank facility: 6 (HCT003-008)
- 6. Tank facility: 4 (LCT019-021, LCT031)

Missing correlations (IV)



JAEA (29 bench. in 3 groups)

- 1. TCA: 5 (LCT062 & rel.)
- 2. STACY: 22 (LST004 & rel.)

3. STACY: 2 (LST012-013)

	LCT	SLCT	SLCT															
	043	044	046	054	058	067	077	082	083	084	088	089	090	091	092	103	002	003
LCT043	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
LCT044	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
LCT046	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+
LCT054	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+	+
LCT058	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+	+
LCT067	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+	+
LCT077	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+	+
LCT082	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+	+
LCT083	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+	+
LCT084	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+	+
LCT088	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+	+
LCT089	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+	+
LCT090	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+	+
LCT091	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+	+
LCT092	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+	+
LCT103	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+	+
SLCT002	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)	+
SLCT003	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	+	(+)

IPEN/MB-01 (18 bench.)

- DICE contains cuantitive data for correlations in k_{eff} experimental uncertainty for 93 benchmark cases:
 - 55 HST cases from IPPE, ORNL and Rocky Flats.
 - 33 cases from ZPR@ANL.
 - 3 cases from VNIIEF and 2 from VNIITE.
- Correlation information for some more systems is available in the literature (obtained by different institutions with different methodologies):
 - 10 MMC/MMCM cases from BFS @IPPE (Ivanova et al. ANE 36 (2009) 305-309).
 - 21 LCT cases from Apparatus-B @CEA Valduc (EG UACSA Benchmark Phase IV).
 - 9 LCT cases from TCA @JAEA (GRS-440).
 - 7 LCT cases from Critical Mass Lab @PNL (W. J. Marshall's Ph. D. Thesis).
- UKAEA & JSI: correlations in shielding benchmarks (ASPIS-Fe88, PCA-REPLICA)
- CEA: correlations in configurations of the EOLE reactor (CAMELEON program)
- Several sets of benchmark experiments with correlated experimental uncertainties in k_{eff} can be identified from DICE. Simulations?



C/E PCA Replica

UKAEA & IJS activities (I)

ASPIS IRON-88 and PCA REPLICA shielding benchmarks

Correlation coefficients among measured reaction rates

 Au, Rh, In, S and Al activation foils installed in 7.4-mm air gaps.

Sensitivity: PCA Replica



(Not to scale)

ASPIS Fe88 Sens

ASPIS-Fe88 covariance matrix for measured RR

Assuming totally correlated power normalisation uncertainty

Det.				Au		R	h	lr.	n i		S		AI
	Pos.	(cm)	26	46	62	26	62	26	46	26	52	62	26
	(cm)	1σ(%)	4,2	4,2	4,2	5,1	5,1	4,5	4,7	6,5	6,5	8,6	4,7
	26	4,2	1	0,95	0,95	0,75	0,75	0,85	0,81	0,59	0,59	0,44	0,81
Au	46	4,2	0,95	1	0,95	0,75	0,75	0,85	0,81	0,59	0,59	0,44	0,81
	62	4,2	0,95	0,95	1	0,75	0,75	0,85	0,81	0,59	0,59	0,44	0,81
Dh	26	5,1	0,75	0,75	0,75	1	0,96	0,7	0,67	0,48	0,48	0,37	0,67
RII	62	5,1	0,75	0,75	0,75	0,96	1	0,7	0,67	0,48	0,48	0,37	0,67
	26	4,5	0,85	0,85	0,85	0,7	0,7	1	0,93	0,55	0,55	0,41	0,76
IN	46	4,7	0,81	0,81	0,81	0,67	0,67	0,93	1	0,52	0,52	0,4	0,72
	26	6,5	0,59	0,59	0,59	0,48	0,48	0,55	0,52	1	0,97	0,73	0,52
S	52	6,5	0,59	0,59	0,59	0,48	0,48	0,55	0,52	0,97	1	0,73	0,52
	62	8,6	0,44	0,44	0,44	0,37	0,37	0,41	0,4	0,73	0,73	1	0,4
AI	26	4,7	0,81	0,81	0,81	0,67	0,67	0,76	0,72	0,52	0,52	0,4	1

ASPIS-Fe88 covariance matrix for measured RR ratios (R_i/R₁)

Det			Au		Rh	In	S		AI
	Patio		A11/A7	A14/A7	A14/A7	A11/A7	A12/A7	A14/A7	A7
	cm/cm	1σ (%)	2,0	2,1	1,8	2,0	2,9	7,7	6,1
Au	46/26	2,0	1	0,5	0				0
	62/26	2,1	0,5	1	0	0	0	0	0
Rh	62/26	1,8	0	0	1	0	0	0	0
In	46/26	2,0	0	0	0	1	0	0	0
S	52/26	2,9	0	0	0	0	1	0,05	0
	62/26	7,7	0	0	0	0	0,05	1	0
AI	26	6,1	0	0	0	0	0	0	1



UKAEA & IJS activities (VI)



Overview of correlations in SFCOMPO

- · Common experimental sources of uncertainty: nuclide vector
 - Use of same methodology (e.g. mass spectrometry or gamma-ray spectrometry)
 - Nuclear data (e.g. gamma-ray emission probabilities, half-lives)
- Common sources of uncertainty in analysis/calculations:
 - Normalisation to BU: $BU = N_f E_f / m_{HM}$; $N_{BI} = N_f \gamma_{BI} \rightarrow$ correlations due to N_{BI} and E_f , γ_{BI} , (exp. + nuclear data)
 - Normalisation to BI: $N_{BI} = N_f \gamma_{BI}$ \rightarrow correlations only due to N_{BI} (experimental data)
- Propagation to calculated nuclide vector:

$$\operatorname{cov}(N_{x,i}, N_{y,j}) = S_{x,i} \operatorname{cov}(N_{BI,i}, N_{BI,j}) S_{y,j}$$
$$S_{x,i} = \frac{\partial N_{x,i}}{\partial N_{BI,i}}$$
$$\operatorname{corr}(N_{x,i}, N_{y,j}) = \operatorname{corr}(N_{BI,i}, N_{BI,j}) = ?$$

x,y – nuclides

- *i*,*j* experiments/benchmarks
- **BI burnup indicator (nuclide)**

CEA activities (I)

Subtask 5.2.1 – Assessing correlations in integral experiments

While a considerable effort has been given to nuclear data covariances in recent years, much less attention has been paid to correlations in integral experiments used in validation, adjustment, and assimilation studies.

Deliverable: Report at M36

- Principle: derive an experimental correlation from uncertainties on common "technological parameters" (fuel enrichment, cell pitch, cladding thickness...) and uncertainties due to the measurement technique
- ▶ Relies on the sensitivities of the considered observables to the technological parameters
- ▶ [1] proposed an expression of the experimental correlation coefficient:

$$r_{i,j} = \frac{S_{TP,i}^{T} \cdot D_{TP} \cdot S_{TP,j} + \varepsilon_{ij}^{2}}{\delta E_{i} \cdot \delta E_{i}}$$

- $S_{TP,i}$ (resp. $S_{TP,j}$) = sensitivity vector of experiment *i* (resp. *j*) to technological parameters - D_{TP} = covariance matrix for technological parameters
- ε_{ij} = uncertainty due to experimental technique if the technique is identical between *i* and *j* 0 otherwise
- δEi (resp. δEj) = total experimental uncertainty

[1]: N. Dos Santos et al., «Impact of mock-up experimental correlations and uncertainties in the transposition process», Proceedings of ANIMMA, 2013

CEA activities (II)

Subtask 5.2.1 – Assessing correlations in integral experiments

While a considerable effort has been given to nuclear data covariances in recent years, much less attention has been paid to correlations in integral experiments used in validation, adjustment, and assimilation studies.

Deliverable: Report at M36

The expression proposed in [1] was tested here on the CAMELEON program on the EOLE mock-up reactor for several physical quantities measured with different experimental techniques on similar core configurations:

i) ρ_{RES} residual reactivity of a mixed UOx / UOx-Gd

ii) Δρ reactivity worth of UOx-Gd

iii) FR fission rate ratio on a fuel pin

▶ Input data to be tested for integral data assimilation

	ρ _{RES}	Δρ	FR
ρ_{RES}	100	63.7	44.5
Δρ		100	0.0
FR			100

[1]: N. Dos Santos et al., «Impact of mock-up experimental correlations and uncertainties in the transposition process», Proceedings of ANIMMA, 2013